

hp calculators

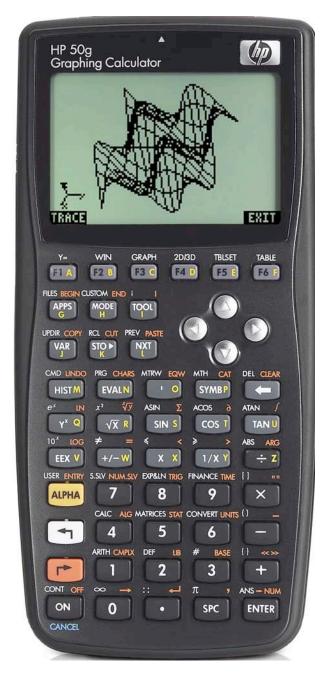
HP 50g Symbolic integration of polynomials

Methods used

The integration commands

The substitution commands

Practice integrating polynomials symbolically



Methods used

The HP50g provides large selection of methods for performing symbolic integration and for finding antiderivatives. Several methods for the symbolic integration of expressions involving polynomials are considered here.

Integration commands

The commands INTVX and RISCH are available in the menu "Derivatives and Integrals" This menu is accessed pressing open the "Calculus" menu.



The first menu item is 1.DERIV & INTEG.... and it is highlighted (selected). In this CHOOSE box selecting 1.DERIV & INTEG... and pressing ENTER or Table 1.DERIV & INTEG... and it is highlighted (selected). In this CHOOSE box selecting 1.DERIV & INTEG... and pressing ENTER or ENTER O



Figure 2

The commands INTVX and RISCH are in the second page of the menu, so you must press \(\mathcal{Z}\) to have the CHOOSE box scroll down and see them. The command INTVX is provided as a shorter way to perform integrations as it only needs one argument, the expression to be integrated, and uses automatically the current CAS variable VX (usually X) as the variable of integration. RISCH needs two arguments: the expression to be integrated and the variable of integration.

Finally, the command Γ is accessible from the keyboard pressing Γ . It needs four arguments: the lower and upper limit of integration, the expression that must be integrated, and the variable of integration. In many cases, this will be the command that is the best choice for numeric integration.

The substitution commands

The commands for substitution are SUBST, | (where), and PREVAL. The command PREVAL allows for the substitution and evaluation of the difference $g(x_2)$ - $g(x_1)$, where g(x) is the antiderivative of some function f(x) that we want to integrate between the limits x_1 and x_2 . This command resides in the menu 1.DERIV & INTEG..... The command SUBST allows for the substitution of the variable of integration,

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since it will take care of altered integration limits and other necessary substitutions in the integral. This command resides in (the second page) of the menu "Algebra" which you access by pressing \overrightarrow{P}

Practice integrating polynomials symbolically

Example 1: Find the antiderivative of the polynomial: $X^4 - 5X^3 + 18X^2 - 60X + 120$

Solution: Assume algebraic exact mode, CHOOSE boxes, and X as the current CAS variable VX. Start the equation writer and call the calculus menu.

EQW (T) CALC



Figure 3

ENTER (Choose the menu 1.DERIV & INTEG.....)



Figure 4

8 (Select the command INTVX)



Figure 5

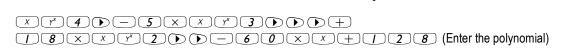
Figure 6

(Put the command INTVX with its place holders in the equation writer)



INTVX()

EDIT CURS BIG . EVAL FACTO SIMP



and perform the integration.

ENTER ENTER

Figure 7

Answer:

$$\frac{1}{5}$$
;× $\frac{5}{5}$ -5; $\frac{1}{4}$;× $\frac{4}{5}$ +18; $\frac{1}{3}$;× $\frac{3}{5}$ -60; $\frac{1}{2}$;× $\frac{2}{5}$ +120;×

Note that since the antiderivative of a function is only determined up to an additive constant, the above result is only one of the possible antiderivatives. The general result is:

$$\tfrac{1}{5} : \times^5 - 5 : \tfrac{1}{4} : \times^4 + 1 : 8 : \tfrac{1}{3} : \times^3 - 60 : \tfrac{1}{2} : \times^2 + 120 : \times + 0$$

where C is the additive constant.

Example 2: Find the antiderivative of:

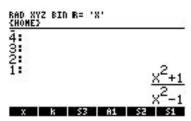


Figure 8

Solution:

Assume RPN exact mode, CHOOSE boxes and X as current variable VX.





Figure 9

CALC ENTER 8 ENTER

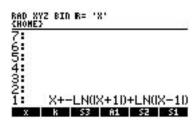
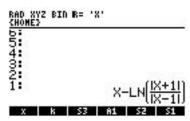


Figure 10

ALG 4 ENTER (Collect the logarithms)



Answer:

Example 3: Integrate symbolically for Y

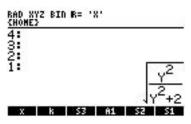


Figure 12

Figure 11

Solution: Assume RPN exact mode with CHOOSE boxes on.

Enter the expression using the EquationWriter.

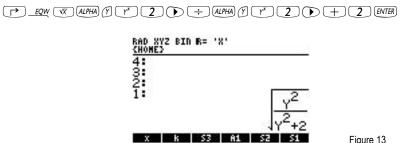


Figure 13

I ALPHA Y ENTER GALC ENTER I VENTER (to find the antiderivative – this takes a few seconds).

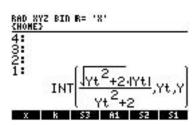
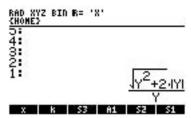


Figure 14

ALG 2 ENTER



Answer:

Example 4: Integrate symbolically:

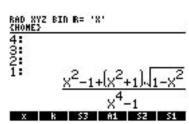
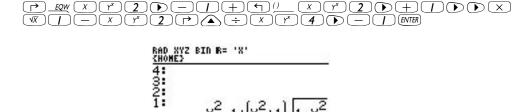


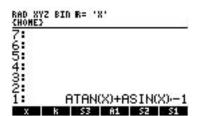
Figure 16

Solution: Assume RPN mode with soft menus and X as the current variable VX. Enter the expression on the stack.



X -1+(X +1)-1-X X 4 -1 X 8 53 61 52 51 Figure 17

(solve the integral)



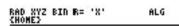
Answer:

Figure 18

<u>Example 5:</u> One physical body moves with $v_x=3t+1$ and $v_y=2$. Find its location vector as a function of time.

Solution: Since $x=J^v(t)dt$ we have to integrate the above velocities v_x and v_y . Assume algebraic mode CHOOSE boxes. Build-up the command.





RISCH([3*t+1,2],t)
x k 53 h1 52 51

Figure 19

ENTER

Answer: